## 2022 PhysicsBowl Answers and Solutions

1. A $\quad \mathrm{KE}_{1}=\mathrm{KE}_{2} ; 1 / 2 \mathrm{~m}_{1} \mathrm{v}_{1}^{2}=1 / 2 \mathrm{~m}_{2} \mathrm{v}_{2}{ }^{2} ; \mathrm{v}_{1}=6.9 \mathrm{~m} / \mathrm{s}$
2. B See: https://www.space.com/20790-eugene-cernan-astronaut-biography.html
3. $\mathbf{C} \quad v=\frac{2 \pi r}{t} ; a=\frac{v^{2}}{r}$
4. B $\quad m v_{\text {before }}=(m+M) v_{\text {after }} ; v_{\text {after }}=\frac{m v_{\text {before }}}{(m+M)}$;
$K E=\frac{1}{2}(m+M) v^{2}{ }_{\text {after }}=\frac{1}{2} \frac{m^{2} v^{2}{ }_{\text {before }}}{(m+M)} ; \mathrm{W}=\mu(m+M) \mathrm{g} \Delta \mathrm{x}$
5. B $\quad v=v_{0}+a t ; \sum \vec{F}=m \vec{a}$
6. D The sum will not equal one of the magnitudes.
7. E Violet: $380-430 \mathrm{~nm}$, Blue: $430-500 \mathrm{~nm}$, Cyan: $500-520 \mathrm{~nm}$, Green: $520-565 \mathrm{~nm}$, Yellow: $565-580 \mathrm{~nm}$, Orange: $580-625 \mathrm{~nm}$, Red: $625-740 \mathrm{~nm}$
8. C $P V=n R T$
9. B KE converted to gravitational potential energy, thermal energy, and work
10. $\mathbf{E} \omega=2 \pi f ; t=\frac{1}{f}=2 \pi \sqrt{\frac{m}{k}} ; \omega=\sqrt{\frac{k}{m}} ; F_{\max }=m \omega^{2} A$
11. E See: https://en.wikipedia.org/wiki/James_E._Webb
12. C $\frac{1.5 \times 10^{9} \mathrm{~m}}{3.0 \times 10^{8} \mathrm{~m} / \mathrm{s}}=5 \mathrm{~s}$
13. A $\mathrm{V}=(\mathrm{l})(\mathrm{A}) ; \mathrm{A}=\pi \mathrm{r}^{2}$
14. D $\tan \theta=\frac{\text { opposite }}{\text { adjacent }}$
15. D $T_{1}=2 \pi \sqrt{\frac{60}{g}} ; T_{2}=2 \pi \sqrt{\frac{63}{g}} ; \mathrm{t}=(\mathrm{n}+1) \mathrm{T}_{1}=\mathrm{nT}_{2}$
16. $\mathrm{C} \quad R=\frac{\rho l}{A} ; \frac{\Delta R}{R}=2 \frac{\Delta l}{l}$
17. E In the absence of friction, all gravitational potential energy will be converted to kinetic energy at the bottom of the plane.
18. C $\Delta x=v_{0} t+\frac{1}{2} a t^{2} ; \mathrm{t}=2$
19. B $\quad F_{\text {air }}=\rho A v ; F_{g}=m g ; \rho A v=m g$
20. D $\quad F_{f}=\mu m g ; F_{g}=m g ; \mu m g=m g$
21. $\mathbf{C} \quad T_{2}=\frac{\left(m_{1}+m_{2}\right) F}{\left(m_{1}+m_{2}+m_{3}\right)}$
22. $\mathbf{E} \quad a_{c}=a_{T}=10 \frac{c m}{s^{2}} ; a_{T}=\omega^{2} r ; \omega=\omega_{0}+\alpha t$
23. B $\quad F_{g}=G \frac{m_{1} m_{2}}{r^{2}} ; F_{e}=k \frac{q_{1} q_{2}}{r^{2}}$
24. $\mathbf{C} \quad T=\sum F=m a+m g$
25. B With a one-wavelength path-length difference, crests will meet crests and troughs will meet troughs.
26. E Only choice with correct values
27. $\mathbf{E} \quad n=\frac{F}{m v}$
28. B $W_{s}=\frac{1}{2} k x^{2} ; W_{f}=\frac{1}{2} m v^{2}-W_{s} ; W_{f}=\mu m g \Delta x$
29. B $\quad P=F v$
30. B $t=\frac{1}{60} s$ for each of the five displacement intervals.
31. B $t_{1}=\sqrt{\frac{2 h}{g}}=0.7 \mathrm{~s} ; t_{2}=0.35 \mathrm{~s} ; \Delta x=\frac{1}{2} g t_{2}{ }^{2}$
32. $\mathbf{E} \quad L=I \omega=\frac{2}{5} M R^{2} \frac{2 \pi}{T}$
33. D $\quad d B=10 \log \left(\frac{I}{I_{0}}\right) ; I_{0}=10^{-12} \frac{\mathrm{~W}}{\mathrm{~m}^{2}}$
34. $\mathbf{C} \quad \sum F=F_{e}+F_{g}=q E+m g$
35. $\mathbf{E} \quad \frac{1}{f}=\frac{1}{d_{0}}+\frac{1}{d_{i}}$
36. A There is no dispersion in a glass block with parallel sides.
37. A $\Delta x_{r e l}=\Delta x-\frac{1}{2} a t^{2}=6 \mathrm{~m} ; v_{r e l}=20 \frac{\mathrm{~m}}{\mathrm{~s}}-16 \frac{\mathrm{~m}}{\mathrm{~s}}=4 \frac{\mathrm{~m}}{\mathrm{~s}} ; a_{r e l}=a_{c a r}-a_{t r u c k}$;

$$
a_{c a r}=a_{t r u c k}+\frac{v_{r e l}^{2}}{2 \Delta x_{r e l}}
$$

38. A With no resistance, $\Delta \mathrm{V}$ will be the same across both components.
39. D $\vec{R}=\sqrt{p^{2}+\left(\frac{4 p}{3}\right)^{2}} ; \tan \theta=\frac{\frac{4 p}{3}}{p}=53^{\circ} ; 180^{\circ}-53^{\circ}=127^{\circ}$
40. D $\quad I_{1} \omega_{1}=(0.8) I_{2} \omega_{2}$
41. $\mathrm{C} \quad \frac{P_{1} V_{1}}{T_{1}}=\frac{P_{2} V_{2}}{T_{2}}$
42. $\mathrm{B} \quad R_{p}=2 \Omega ; R_{\text {total }}=5 \Omega ; \mathrm{V}=\mathrm{IR} ; \mathrm{I}=24 \mathrm{~A}$
43. B $\quad n_{1} \sin \Theta_{1}=n_{2} \sin \Theta_{2}$
44. C $\quad N(t)=N_{0}\left(\frac{1}{2}\right)^{\frac{t}{t_{1} / 2}}$
45. B $\quad q E=q v B$
46. B The electric fields are pointed in opposite directions ( $45^{\circ}$ and $225^{\circ}$ from the x -axis) and therefore cancel each other out. Since each arc is a collection of point charges located the same distance from the origin, then: $V=\frac{k Q}{R}$. Both arcs create positive potentials, so $V=2\left(\frac{k Q}{R}\right)$.
47. A $\quad F=F_{f}-F_{g}=\mu m g \cos \theta-m g \sin \theta$
48. D Combination Z , with three resistors in parallel, offers the least amount of resistance. Combination X, with two resistors in parallel and one in series, offers the most resistance.
49. C There are three main factors to consider here. The gravitational constant, $G$, the mass of the sun, $M$, and the distance between the sun and the earth, $R$. The units of $G$ are $\frac{m^{3}}{(k g) s^{2}}$, the units of $M$ are $k g$, the units of $R$ are $m$, and we want to solve for time in seconds. Using dimensional analysis to solve for seconds, we get Time $=\sqrt{\frac{R^{3}}{G M}}=5.1 \times 10^{6}$ seconds $=59$ days. Using calculus, one arrives at 64.5 days.
50. C $\quad P V=n R T$; At the end of Stage 1: $\mathrm{P}=5.05 \times 10^{4} \mathrm{~Pa}, \mathrm{~V}=2 \mathrm{~m}^{3}$, and $\mathrm{T}=273.15 \mathrm{~K}$. At The end of Stage $2, \mathrm{P}=1.01 \times 10^{5} \mathrm{~Pa}, \mathrm{~V}=2 \mathrm{~m}^{3}$, and $\mathrm{T}=546.3 \mathrm{~K} . \mathrm{n}=44.3 \mathrm{~mol}$ through the entire problem. Work done in Stage 3: $\mathrm{W}_{3}=\mathrm{P}_{3}\left(\mathrm{~V}_{1}-\mathrm{V}_{3}\right)$.
