

(1) Can a helium balloon lift the tank the helium came in?

A spherical tank of radius  $a$ , wall thickness  $t$ , and density  $\rho_{\text{wall}}$  weighs  $4\pi a^2 t g \rho_{\text{wall}}$ ; if it contains helium at pressure  $P$ , the stress on the wall is  $S = aP / t$ . At atmospheric pressure  $P_0$  the helium displaces air weighing  $(4\pi/3)a^3 g \rho_{\text{air}} (P / P_0)$ . If this equals the tank weight then  $S = (3/2)P_0 (\rho_{\text{wall}} / \rho_{\text{air}}) = 150\,000$  psi for steel *independent* of  $a$ ,  $t$ , and  $P$ . The stress would be twice as large for a cylindrical tank. The answer is no. Steel is not strong enough.